

# BOARD QUESTION PAPER: MARCH 2019

## MATHS (PART - II)

Time: 2 Hours

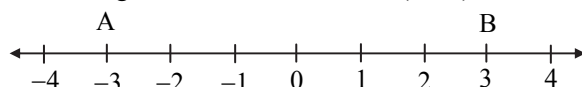
Max. Marks: 40

**Note:**

- i. All questions are compulsory.
- ii. Use of calculator is not allowed.
- iii. Figures to the right of questions indicate full marks.
- iv. Draw proper figures for answers wherever necessary.
- v. The marks of construction should be clear and distinct. Do not erase them.
- vi. While writing any proof, drawing relevant figure is necessary. Also the proof should be consistent with the figure.

1. (A) Solve the following questions (Any four): [4]

- i. If  $\triangle ABC \sim \triangle PQR$  and  $\angle A = 60^\circ$ , then  $\angle P = ?$
- ii. In right-angled  $\triangle ABC$ , if  $\angle B = 90^\circ$ ,  $AB = 6$ ,  $BC = 8$ , then find  $AC$ .
- iii. Write the length of largest chord of a circle with radius 3.2 cm.
- iv. From the given number line, find  $d(A, B)$ :



- v. Find the value of  $\sin 30^\circ + \cos 60^\circ$ .
- vi. Find the area of a circle of radius 7 cm.

(B) Solve the following questions (Any two): [4]

- i. Draw seg  $AB$  of length 5.7 cm and bisect it.
- ii. In right-angled triangle  $PQR$ , if  $\angle P = 60^\circ$ ,  $\angle R = 30^\circ$  and  $PR = 12$ , then find the values of  $PQ$  and  $QR$ .
- iii. In a right circular cone, if perpendicular height is 12 cm and radius is 5 cm, then find its slant height.

2. (A) Choose the correct alternative: [4]

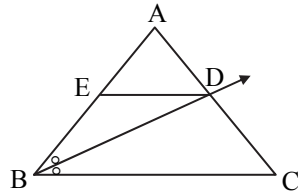
- i.  $\triangle ABC$  and  $\triangle DEF$  are equilateral triangles. If  $A(\triangle ABC) : A(\triangle DEF) = 1 : 2$  and  $AB = 4$ , then what is the length of  $DE$ ?  
 (A)  $2\sqrt{2}$       (B) 4      (C) 8      (D)  $4\sqrt{2}$
- ii. Out of the following which is a Pythagorean triplet?  
 (A) (5, 12, 14)    (B) (3, 4, 2)      (C) (8, 15, 17)    (D) (5, 5, 2)
- iii.  $\angle ACB$  is inscribed in arc  $ACB$  of a circle with centre  $O$ . If  $\angle ACB = 65^\circ$ , find  $m(\text{arc } ACB)$ :  
 (A)  $130^\circ$       (B)  $295^\circ$       (C)  $230^\circ$       (D)  $65^\circ$
- iv.  $1 + \tan^2 \theta = ?$   
 (A)  $\sin^2 \theta$       (B)  $\sec^2 \theta$       (C)  $\operatorname{cosec}^2 \theta$     (D)  $\cot^2 \theta$

(B) Solve the following questions (Any two): [4]

- i. Construct tangent to a circle with centre  $A$  and radius 3.4 cm at any point  $P$  on it.
- ii. Find slope of a line passing through the points  $A(3, 1)$  and  $B(5, 3)$ .
- iii. Find the surface area of a sphere of radius 3.5 cm.

3. (A) Complete the following activities (Any two):

i.



In  $\triangle ABC$ , ray BD bisects  $\angle ABC$ .

If  $A-D-C$ ,  $A-E-B$  and  $\text{seg } ED \parallel \text{side } BC$ , then prove that:  $\frac{AB}{BC} = \frac{AE}{EB}$ .

**Proof:**

In  $\triangle ABC$ , ray BD is bisector of  $\angle ABC$ .

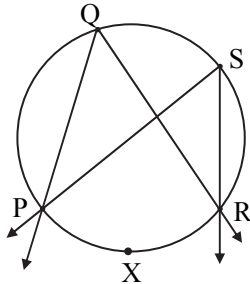
$\therefore \frac{AB}{BC} = \frac{AD}{DC}$  ... (i) (By angle bisector theorem)

In  $\triangle ABC$ ,  $\text{seg } DE \parallel \text{side } BC$

$\therefore \frac{AE}{EB} = \frac{AD}{DC}$  ... (ii)

$\therefore \frac{AB}{BC} = \frac{AE}{EB}$  ... [From (i) and (ii)]

ii.



Prove that, angles inscribed in the same arc are congruent.

**Given:**  $\angle PQR$  and  $\angle PSR$  are inscribed in the same arc.  
Arc PXR is intercepted by the angles.

**To prove:**  $\angle PQR \cong \angle PSR$

**Proof:**

$m\angle PQR = \frac{1}{2} m(\text{arc } PXR)$  ... (i)

$m\angle \text{  } = \frac{1}{2} m(\text{arc } PXR)$  ... (ii)

$\therefore m\angle \text{  } = m\angle PSR$  ... [From (i) and (ii)]

$\therefore \angle PQR \cong \angle PSR$  ... (Angles equal in measure are congruent)

iii. How many solid cylinders of radius 6 cm and height 12 cm can be made by melting a solid sphere of radius 18 cm?

**Activity:** Radius of the sphere,  $r = 18$  cm

For cylinder, radius  $R = 6$  cm, height  $H = 12$  cm

$\therefore$  Number of cylinders can be made =  $\frac{\text{Volume of the sphere}}{\text{  }}$

=  $\frac{4}{3} \pi r^3$

=  $\frac{4}{3} \times 18 \times 18 \times 18$

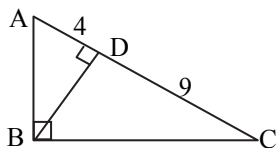
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(B) Solve the following questions (Any two):

[4]

i.



In right-angled  $\triangle ABC$ ,  $BD \perp AC$ .

If  $AD = 4$ ,  $DC = 9$ , then find  $BD$ .

ii. Verify whether the following points are collinear or not:

$A(1, -3)$ ,  $B(2, -5)$ ,  $C(-4, 7)$ .

iii. If  $\sec \theta = \frac{25}{7}$ , then find the value of  $\tan \theta$ .

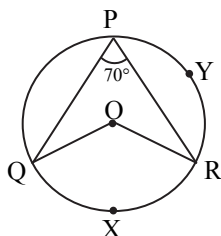


4. Solve the following questions (Any three):

[9]

i. In  $\triangle PQR$ , seg  $PM$  is a median,  $PM = 9$  and  $PQ^2 + PR^2 = 290$ . Find the length of  $QR$ .

ii.



In the given figure,  $O$  is centre of circle.  $\angle QPR = 70^\circ$  and  $m(\text{arc } PYR) = 160^\circ$ , then find the value of each of the following:

(a)  $m(\text{arc } QXR)$

(b)  $\angle QOR$

(c)  $\angle PQR$

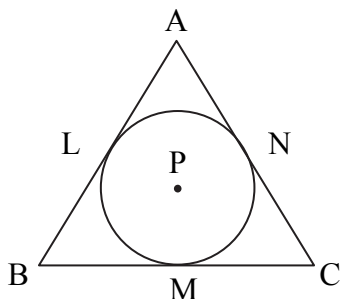
iii. Draw a circle with radius 4.2 cm. Construct tangents to the circle from a point at a distance of 7 cm from the centre.

iv. When an observer at a distance of 12 m from a tree looks at the top of the tree, the angle of elevation is  $60^\circ$ . What is the height of the tree? ( $\sqrt{3} = 1.73$ )

5. Solve the following questions (Any one):

[4]

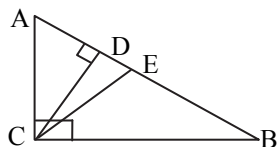
i.



A circle with centre  $P$  is inscribed in the  $\triangle ABC$ . Side  $AB$ , side  $BC$  and side  $AC$  touch the circle at points  $L$ ,  $M$  and  $N$  respectively. Radius of the circle is  $r$ .

Prove that:  $A(\triangle ABC) = \frac{1}{2} (AB + BC + AC) \times r$ .

ii.



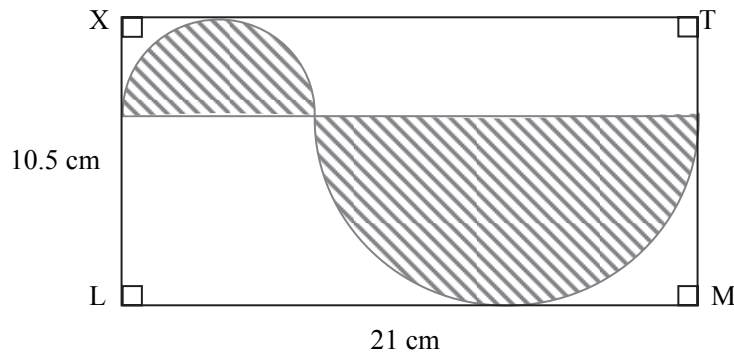
In  $\triangle ABC$ ,  $\angle ACB = 90^\circ$ . seg  $CD \perp$  side  $AB$  and seg  $CE$  is angle bisector of  $\angle ACB$ .

Prove that:  $\frac{AD}{BD} = \frac{AE^2}{BE^2}$ .

## 6. Solve the following questions (Any one):

[3]

- i. Show that the points  $(2, 0)$ ,  $(-2, 0)$  and  $(0, 2)$  are the vertices of a triangle. Also state with reason the type of the triangle.
- ii.



In the above figure,  $\square XLMT$  is a rectangle.  $LM = 21$  cm,  $XL = 10.5$  cm. Diameter of the smaller semicircle is half the diameter of the larger semicircle. Find the area of non-shaded region.

